

A FUZZY COOPERATIVE GENETIC ALGORITHM
FOR FUZZY MODELING

MOHD ARFIAN BIN ISMAIL

UNIVERSITI TEKNOLOGI MALAYSIA

A FUZZY COOPERATIVE GENETIC ALGORITHM
FOR FUZZY MODELING

MOHD ARFIAN BIN ISMAIL

A thesis submitted in fulfillment of the
requirements for the award of the degree of
Master of Science (Computer Science)

Faculty of Computer Science and Information Systems
Universiti Teknologi Malaysia

MAY 2011

To everyone who miss me while I'm working on this work

ACKNOWLEDGEMENTS

I would like to express my true and sincere thanks and gratitude to my supervisor, Dr Hishammuddin bin Asmuni for his patience, guidance, encouragement, invaluable comments, and advice that made this research possible and completed early.

I would like to thank all members of the Laboratory of Computational Intelligence and Biotechnology (LCIB) for their continuous support in many aspects of this research especially Dr. Muhamad Razib bin Othman.

Most importantly, my deepest thanks go to my parent. Their influence made me realize the importance of education from a very early age. I cannot give enough thanks to my parent for the great love and support that they has been giving me throughout my life.

ABSTRACT

Fuzzy modeling refers to the process of identifying the fuzzy parameters by defining fuzzy rules and fuzzy sets. The process of identifying the fuzzy parameters becomes complicated and difficult to evaluate particularly when it involves complex problems in engineering and medical applications. This is due to the fact that there are many fuzzy parameters to be identified such as the characteristics of the fuzzy rules and fuzzy sets. Besides that, the accuracy and the ability to interpret the fuzzy rules and the fuzzy sets would also need to be considered. This study proposes an improved method of fuzzy modeling called the Fuzzy Cooperative Genetic Algorithm (FCoGA) which integrates the Genetic Algorithm (GA) and Cooperative Coevolution Algorithm (CooCEA) that automatically generate and refine the fuzzy rules and the fuzzy sets. The GA is used to exploit the chromosomes that represent the fuzzy parameters whereas the CooCEA is applied to reduce the complexity of the fuzzy parameters representation which is carried out by subdividing chromosomes into three sub-chromosomes known as species. The FCoGA comprises of three phases which are simplification, tuning and evaluation. Simplification phase involves decomposition of the chromosomes into three species of chromosomes that represent the fuzzy parameters consisting of fuzzy rules, membership functions and length of the overlapping membership functions. The tuning phase involves the process of altering and tuning all the species. Lastly, the evaluation phase validates the performance of the FCoGA. Three benchmark datasets; breast cancer, diabetes and Iris have been used to evaluate the performance of the FCoGA. The experimental results showed that the FCoGA obtained the highest percentage of accuracy classification compared to other techniques such as conventional GA, multi-objective CooCEA, rule extraction and decision tree. The results also indicated that the FCoGA produced higher interpretability of a fuzzy model.

ABSTRAK

Permodelan kabur merujuk kepada proses mengenal pasti parameter kabur dengan memberi definisi terhadap peraturan-peraturan kabur dan set-set kabur. Terdapat beberapa masalah di dalam permodelan kabur apabila ia digunakan pada masalah yang kompleks di mana ia menyebabkan proses mengenal pasti parameter kabur menjadi rumit dan sukar untuk dinilai. Ini disebabkan proses mengenal pasti parameter kabur yang terlalu banyak seperti ciri-ciri peraturan-peraturan kabur dan set-set kabur. Selain itu, ketepatan dan kemampuan untuk mentafsir model kabur juga perlu diambil kira. Kajian ini mencadangkan satu kaedah automatik bagi permodelan kabur yang diberi nama Algoritma Genetik Kerjasama Kabur (FCoGA) yang menggabungkan Algoritma Genetik (GA) dan Algoritma Evolusi yang Bekerjasama (CooCEA) di mana ia dapat menjana dan memperbaiki peraturan-peraturan kabur dan set-set kabur secara automatik. GA menggunakan kromosom untuk mewakili parameter kabur manakala CooCEA digunakan untuk meringkaskan perwakilan penyelesaian yang terlalu kompleks dengan memecahkan kromosom kepada tiga sub-kromosom yang dikenali sebagai spesies. Terdapat tiga fasa utama di dalam FCoGA iaitu memudahkan, mengubah, dan menilai. Fasa memudahkan adalah proses pemecahan kromosom kepada tiga spesies yang mewakili parameter kabur; peraturan kabur, fungsi keahlian dan panjang pertindihan fungsi keahlian. Fasa mengubah melibatkan proses mengubah dan memperbaiki semua spesies. Akhir sekali, fasa menilai pula ialah proses penilaian prestasi FCoGA. Di dalam proses menilai, tiga piawaian set data iaitu barah payudara, diabetes dan bunga telah digunakan. Hasil analisis menunjukkan bahawa FCoGA dapat mencapai ketepatan pengelasan yang tinggi berbanding dengan kaedah-kaedah lain di dalam permodelan kabur seperti GA yang biasa, CooCEA yang mempunyai banyak objektif, pencabutan peraturan dan pokok keputusan. Di samping itu, FCoGA berupaya untuk menjana model kabur yang mudah untuk difahami.

TABLE OF CONTENTS

| CHAPTER | TITLE | PAGE |
|----------|----------------------------------|----------|
| | DECLARATION | ii |
| | DEDICATION | iii |
| | ACKNOWLEDGEMENTS | iv |
| | ABSTRACT | v |
| | ABSTRAK | vi |
| | TABLE OF CONTENTS | vii |
| | LIST OF TABLES | xi |
| | LIST OF FIGURES | xiii |
| | LIST OF ABBREVIATIONS | xv |
| | LIST OF APPENDICES | xvii |
| 1 | INTRODUCTION | 1 |
| | 1.1 Background | 1 |
| | 1.2 Challenges in Fuzzy Modeling | 3 |
| | 1.3 Statement of the Problem | 4 |
| | 1.4 Objectives of the Study | 5 |
| | 1.5 Scope of the Study | 6 |
| | 1.6 Significance of the Study | 7 |
| | 1.7 Structure of the Thesis | 7 |
| 2 | LITERATURE REVIEW | 9 |
| | 2.1 Introduction | 9 |

| | | |
|----------|--|-----------|
| 2.2 | Fuzzy System | 10 |
| 2.3 | Fuzzy Modeling | 13 |
| 2.4 | Bio-inspired Approach for Fuzzy Modeling | 15 |
| 2.4.1 | Genetic Algorithm | 20 |
| 2.4.2 | Evolutionary Programming | 21 |
| 2.4.3 | Evolutionary Strategy | 22 |
| 2.4.4 | Genetic Programming | 22 |
| 2.5 | Genetic Algorithm in Fuzzy Modeling | 23 |
| 2.5.1 | Genetic Fuzzy System | 24 |
| 2.5.2 | Genetic Fuzzy Rule-Based System | 25 |
| 2.6 | Coevolutionary Algorithm | 31 |
| 2.6.1 | Competitive Coevolutionary Algorithm | 32 |
| 2.6.2 | Cooperative Coevolutionary Algorithm | 33 |
| 2.6.3 | Cooperative Coevolutionary Algorithm with Genetic Fuzzy Rule-Based System | 34 |
| 2.7 | Trends and Tendencies | 36 |
| 2.8 | Summary | 38 |
| 3 | RESEARCH METHODOLOGY | 39 |
| 3.1 | Introduction | 39 |
| 3.2 | Research Activity | 40 |
| 3.3 | The Proposed Method | 42 |
| 3.4 | Data Source | 44 |
| 3.4.1 | Iris Dataset | 44 |
| 3.4.2 | Pima Indian Diabetes Dataset | 45 |
| 3.4.3 | Wisconsin Breast Cancer Diagnosis Dataset | 46 |
| 3.5 | Experimental Environment | 47 |
| 3.5.1 | The Requirements in Hardware and Software | 48 |
| 3.5.2 | Testing and Analyzing | 48 |
| 3.6 | Summary | 50 |

| | | |
|----------|--|-----------|
| 4 | FUZZY COEVOLUTIONARY GENETIC ALGORITHM FOR FUZZY MODELING | 51 |
| 4.1 | Introduction | 51 |
| 4.2 | Steps in Fuzzy Cooperative Genetic Algorithm | 52 |
| 4.3 | Cooperative Chromosome Representation | 55 |
| 4.4 | Fitness Evaluation | 60 |
| 4.5 | Classification by Fuzzy System | 63 |
| 4.6 | Selection | 64 |
| 4.7 | Reproduction | 65 |
| 4.8 | Summary | 67 |
| 5 | RESULT AND DISCUSSION | 69 |
| 5.1 | Introduction | 69 |
| 5.2 | Sensitivity Analyses | 70 |
| 5.2.1 | Population Size | 70 |
| 5.2.2 | Crossover Probability | 71 |
| 5.2.3 | Mutation Probability | 72 |
| 5.2.4 | Elite Probability | 73 |
| 5.2.5 | Number of Rules | 74 |
| 5.3 | Experimental Results | 75 |
| 5.3.1 | Result of Iris Dataset | 79 |
| 5.3.2 | Result of Pima Indian Diabetes Dataset | 81 |
| 5.3.3 | Result of Wisconsin Breast Cancer Diagnosis Dataset | 85 |
| 5.4 | Discussion | 86 |
| 5.5 | Summary | 93 |
| 6 | CONCLUSION | 94 |
| 6.1 | Concluding Remarks | 94 |
| 6.2 | Contributions | 96 |
| 6.3 | Future Works | 97 |
| 6.4 | Dissemination | 98 |
| 6.5 | Summary | 99 |

REFERENCES

100

APPENDICES A-D

112 – 133

LIST OF TABLES

| TABLE NO. | TITLE | PAGE |
|-----------|--|------|
| 2.1 | Description of the components in fuzzy system | 11 |
| 2.2 | Current works that used Evolutionary Algorithm in fuzzy modeling | 19 |
| 2.3 | Genetic tuning approach | 27 |
| 2.4 | Genetic learning approach | 27 |
| 3.1 | Iris dataset | 45 |
| 3.2 | Pima Indian Diabetes dataset | 46 |
| 3.3 | Wisconsin Breast Cancer Diagnosis dataset | 47 |
| 3.4 | Parameters setting | 49 |
| 5.1 | The effect of population size | 71 |
| 5.2 | The effect of crossover probability | 72 |
| 5.3 | The effect of mutation probability | 73 |
| 5.4 | The effect of elite probability | 74 |
| 5.5 | Comparison of using elite concept | 74 |
| 5.6 | The effect of the number of rules | 75 |
| 5.7 | The best parameter settings obtain by Fuzzy Cooperative Genetic Algorithm after several sensitivity analyses | 76 |
| 5.8 | A summary result obtained by Fuzzy Cooperative Genetic Algorithm | 77 |

| | | |
|------|--|----|
| 5.9 | The full result of Fuzzy Cooperative Genetic Algorithm | 78 |
| 5.10 | A comparison of the result obtained when applied on Iris dataset to other publishes technique | 80 |
| 5.11 | A comparison of the result obtained when applied on Pima Indian Diabetes dataset to other publishes technique | 83 |
| 5.12 | A comparison of the result obtained when applied on Wisconsin Breast Cancer Diagnosis dataset to other publishes technique | 85 |
| 5.13 | A comparison of one fitness level with two fitness levels | 88 |

LIST OF FIGURES

| FIGURE NO. | TITLE | PAGE |
|------------|--|------|
| 2.1 | Components in a fuzzy system | 11 |
| 2.2 | Main process in a fuzzy system | 12 |
| 2.3 | Pseudo-code for a sequential Evolutionary Algorithm | 16 |
| 2.4 | The idea of Genetic Fuzzy System | 25 |
| 2.5 | Process of genetic rule learning | 29 |
| 2.6 | Process of genetic selection of rule sets | 29 |
| 2.7 | Process of genetic Data Base learning | 30 |
| 2.8 | Simultaneous genetic learning of Data Base and Rule Base | 30 |
| 2.9 | Framework of Cooperative Coevolutionary Algorithm | 34 |
| 3.1 | The flow of the research activities | 41 |
| 3.2 | The proposed method | 43 |
| 4.1 | Pseudo-code of Fuzzy Cooperative Genetic Algorithm | 52 |
| 4.2 | Steps involve in Fuzzy Cooperative Genetic Algorithm | 54 |
| 4.3 | Overview of species in Fuzzy Cooperative Genetic Algorithm | 56 |
| 4.4 | The process encode of S_{FR} | 58 |
| 4.5 | The process encode of S_{MF} and S_{RG} | 59 |
| 4.6 | Fitness evaluation in Fuzzy Cooperative Genetic Algorithm | 62 |
| 4.7 | Concept of elite selection | 64 |

| | | |
|------|--|----|
| 4.8 | Crossover on every species | 66 |
| 4.9 | Mutation on every species | 67 |
| 5.1 | The best of the fuzzy rules when applied on Iris dataset | 80 |
| 5.2 | The best of the fuzzy sets when applied on Iris dataset | 82 |
| 5.3 | The best of the fuzzy rules when applied on Pima Indian Diabetes dataset | 84 |
| 5.4 | The best of the fuzzy sets when applied on Pima Indian Diabetes dataset | 84 |
| 5.5 | The best of the fuzzy rules when applied on Wisconsin Breast Cancer Diagnosis dataset | 86 |
| 5.6 | The best of the fuzzy sets when applied on Wisconsin Breast Cancer Diagnosis dataset | 87 |
| 5.7 | Speed of learning on Iris dataset | 89 |
| 5.8 | Speed of learning on Pima Indian Diabetes dataset | 90 |
| 5.9 | Speed of learning on Wisconsin Breast Cancer Diagnosis dataset | 90 |
| 5.10 | Comparison of speed of learning on Iris dataset | 91 |
| 5.11 | Comparison of speed of learning on Pima Indian Diabetes dataset | 92 |
| 5.12 | Comparison of speed of learning on Wisconsin Breast Cancer Diagnosis dataset | 92 |

LIST OF ABBREVIATIONS

| | | |
|--------|---|--------------------------------------|
| ANN | – | Artificial Neural Networks |
| AR | – | Auto-Regressive |
| BNN | – | Biological neural networks |
| BOA | – | Bisector of Area |
| CEA | – | Coevolutionary Algorithm |
| COG | – | Center of Gravity |
| ComCEA | – | Competitive Coevolutionary Algorithm |
| CooCEA | – | Cooperative Coevolution Algorithm |
| DB | – | Data Base |
| EA | – | Evolutionary Algorithm |
| EP | – | Evolutionary Programming |
| ES | – | Evolutionary Strategy |
| FCoGA | – | Fuzzy Cooperative Genetic Algorithm |
| GA | – | Genetic Algorithm |
| GFRBS | – | Genetic Fuzzy Rules Base System |
| GFS | – | Genetic Fuzzy System |
| GP | – | Genetic Programming |
| IDE | – | Integrated Development Environment |
| KB | – | Knowledge Base |
| MOM | – | Mean of Maxima |
| NIC | – | Network Interface Card |
| NN | – | Neural Network |

| | | |
|--------|---|--|
| PID | – | Pima Indian Diabetes |
| RAM | – | Random Access Memory |
| RB | – | Rule Base |
| SFE | – | Sozonov Fuzzy Engine |
| SOFRGP | – | Self-Organized Fuzzy Rule Generation Procedure |
| UCI | – | University of California, Irvine |
| WBCD | – | Breast Cancer Diagnosis |

LIST OF APPENDICES

| FIGURE NO. | TITLE | PAGE |
|-------------------|--|-------------|
| A | Iris dataset | 112 |
| B | PIMA Indian Diabetes (PID) dataset | 114 |
| C | Wisconsin Breast Cancer Diagnosis (WBCD) dataset | 121 |
| D | Encoding Process of Species | 128 |

CHAPTER 1

INTRODUCTION

1.1 Background

In many decision-making environments, there are several factors that need to be considered in order to ensure the optimum solution can be achieved. Sometimes, the factors that are to be taken into consideration are unknown and uncertain. This situation happened due to the lack of expert knowledge or the absence of expertise (Stephanou and Sage, 1987; Negnevitsky, 2002). In acquiring the expert knowledge, it involves many knowledge-processing procedures. The knowledge from many different experts needs to be collected and organized. In addition, it is vital to formalize the knowledge before applying it to the problem. However, acquiring the expert knowledge is costly and the process of collecting the knowledge is time consuming. Dealing with this situation, using an expert system is a good choice. An expert system is a computer program that is built with the expert knowledge in order to solve a specific problem. There are two approaches in obtaining the knowledge which are the knowledge derived from the experts or by extracting the knowledge from available data. As the process of acquiring the experts' knowledge is time consuming and costly, to obtain the expertise's knowledge also involves many

procedures. On the other hand, the process of extracting the knowledge from the data is more efficient in terms of the lesser cost and shortens the time of performing it. Through data collection, a scientist can extract and interpret knowledge in the data in order to determine the pattern of the data, to find out the parameter that contains in the data and their relationship, to predict the physical and environment of the nature, and also to make a better decision based on the knowledge contained in the data. It works through the process of learning, extracting and presenting the knowledge in the form that is acceptable by human. However, several issues will arise when the data is inaccurate and incomplete which can result the knowledge to be imprecise, uncertain, or unreliable. Due to that, the fuzzy system is seen as a good choice to deal with these issues where it is used to represent and highlight the knowledge that is imprecise, uncertain and unreliable (Tsipouras *et al.*, 2008; Gadaras and Mikhailov, 2009).

Fuzzy system works by implementing the fuzzy logic and approximate reasoning, as well as incorporating the expert knowledge in the inference system in order to obtain the desired output from the system input values (Wang, 1997). In developing the fuzzy system, fuzzy parameters are needed to be identified in order to obtain the desired behavior of the system. This process is known as the fuzzy modeling (Reyes and Sipper, 2002; Cordon *et al.*, 2004). Fuzzy system works well on simple problems, but when applied on complex problems like engineering (Pulkkinen *et al.*, 2008; Mendonca *et al.*, 2009; Wang *et al.*, 2009) or medical problems (Ghazavi and Liao, 2008; Stylios *et al.*, 2008; Gadaras and Mikhailov, 2009), the construction of the fuzzy system becomes complicated. This might be due to the identification of many fuzzy parameters. Due to that, a method is needed for identifying the fuzzy parameters where an automatic process to identifying the fuzzy parameters is performed.

The following section will describe the challenges that arise in the fuzzy modeling in details followed by a review about the statement of the problems of this study. Next, the objectives of this study are presented. Lastly, the significance and scope of the study are discussed.

1.2 Challenges in Fuzzy Modeling

The process of building the fuzzy system is a hard process, especially for real-problems. This is because of the identifying process of the parameters that is crucial where it has influences on the performance of the system (Chen *et al.*, 2007; Zong-Yi *et al.*, 2008; Gadaras and Mikhailov, 2009). Generally, the fuzzy parameter that needs to be identified is the fuzzy model which refers to a collection of fuzzy rules and fuzzy sets. Before the fuzzy model is identified, several factors need to be considered. For the fuzzy rules, the factors are the number of rules, the antecedent and consequence, and the linguistic variable and the linguistic value. For the fuzzy set, the factors are the number of membership function, the types of membership function and the shape of membership function. These factors need to be considered in order to produce the fuzzy rules and fuzzy sets with more accurate and more interpretable. Furthermore, it turns out to be difficult because of the computation grows exponentially together with the increase of the number of variables in the system especially for the real world problems. This problem is known as the *curse of dimensionality* which is a major problem in the development of the fuzzy system (Reyes and Sipper, 2002). Therefore, this problem becomes the first challenge in this study. In dealing with this problem, an automatic approach in the fuzzy modeling is proposed.

There are many techniques that can be applied to automate the fuzzy modeling. Current trend shows that Evolutionary Algorithm (EA) is the most popular technique that is being used, especially the Genetic Algorithm (GA: Kim and Ryu, 2005; Kelesoglu, 2007; Dimitriou *et al.*, 2008; Li *et al.*, 2008; Evsukoff *et al.*, 2009; Li and Wang, 2009). Most of the works combine a fuzzy system with GA because of the good learning capabilities offered in solving problems. GA can be viewed as a search technique where the goal is to find the exact or approximate solution for the optimization problems. GA performs well in optimization problems, but when it is applied in complex problems such as when many dimensions of data (Luukka, 2009), when the value of data in a big range (Hong *et al.*, 2008; Alcala-Fdez *et al.*, 2009), when the search space is large (Li and Wang, 2009), involve multi-classification

problem (Har-Peled *et al.*, 2002; Brinker *et al.*, 2006) and involve many parameters setting (Lau *et al.*, 2009), it tends to stuck in the local optima and thus performs poorly (Wang, 1997). With complex problem, it requires high computation power due to the representation of the solution. This happened due to the identification of many factors of fuzzy parameter such as the number of fuzzy parameters and their characteristics, where it makes the representation of the solution become complex. As a result, this might have contributed to the loss of the interpretability of the fuzzy model where the fuzzy model maybe becomes unreliable and uncertain. In addition, to evaluate the solution, time is very consuming. Therefore, there is a need to embody a method to simplify the representation of the solution in the interest of avoiding the fuzzy model to lose its interpretability. Derived from this situation, another challenge in the fuzzy modeling is to employ a decomposition method, which is the Cooperative Coevolutionary Algorithm (CooCEA) into GA (Potter and Jong, 2000; Reyes and Sipper, 2002; Xing *et al.*, 2007; Yang *et al.*, 2008; Zhu and Guan, 2008; Xing *et al.*, 2009). By implementing this technique, it is hoped that the CooCEA can reduce the complexity of the representation of the solution in order to improve the interpretability of the model.

1.3 Statement of the Problem

In fuzzy modeling, the identification of the parameters in the fuzzy system is essential for its operation. These parameters affect the performance of the system. Therefore, it is become a problem in fuzzy modeling because several factors must be considered in order to develop the fuzzy system. These factors are the accuracy of the results and interpretability of the fuzzy model (Xing *et al.*, 2007; Evsukoff *et al.*, 2009). These factors become important issues in the fuzzy modeling because it needs to deal with these factors at the same time. As a consequence, it is a difficult process to design a method of the fuzzy modeling in dealing with the accuracy and interpretability at the same time. Moreover, the extraction of the knowledge in the

data can be difficult if the data is limited, complex, inaccurate and incomplete (Yang *et al.*, 2008; Fernandez *et al.*, 2009). This is the second problem in the fuzzy modeling which can make the knowledge obtained to be imprecise, wrong or simply uncertain (Tsipouras *et al.*, 2008; Gadaras and Mikhailov, 2009). Therefore, there is a need for a technique where it can automatically adjust, alter and fine-tune the knowledge in order to assure the specific requirement achieved. Besides that, a major problem in the fuzzy modeling is the *curse of dimensionality*. This happened due to the demand in the identification process of the many fuzzy parameters when it is applied on large search space and complex systems (Reyes and Sipper, 2002). The problems in fuzzy modeling can be summarized as follows:

- (i) An automated approach in fuzzy modeling is needed to automatically alter, adjust and tune the fuzzy parameters.
- (ii) Identification of many factors of fuzzy parameters such as number of fuzzy model and its characteristic.
- (iii) Constraint of the data when data is limited, complex, inaccurate and incomplete.

1.4 Objectives of the Study

The main goal of this study is to develop a method that can automatically generate the ‘best’ of the fuzzy models that took into account the accuracy and interpretability of the model, and can achieve a better result when it is applied on the classification data. For that specific purpose, the following objectives need to be accomplished:

- (i) To develop an algorithm named Fuzzy Cooperative Genetic Algorithm (FCoGA) for fuzzy modeling by incorporating GA with the CooCEA.

- (ii) To generate fuzzy model that has a higher interpretability by using the CooCEA that decomposed the representation of the solution (cooperative chromosome) into sub-solutions (species).
- (iii) To propose fuzzy modeling method that is able to achieve a higher accuracy of the classification by introducing two levels of fitness evaluation which are at the species level and cooperative chromosome level.

1.5 Scope of the Study

In this study, three datasets are used, particularly the Iris dataset, Pima Indian Diabetes (PID) dataset and Wisconsin Breast Cancer Diagnosis (WBCD) dataset. These datasets are obtained from the UCI machine learning repository. The scopes of the proposed method are as follows:

- (i) The scope of the proposed method is focusing on the classification.
- (ii) Use GA and CooCEA to randomly generate the initial population into three species that represented the fuzzy parameters where the fuzzy parameters are fuzzy rules, fuzzy sets and the length overlap in fuzzy sets.
- (iii) In the interest of evaluating the performance of the proposed method, k -fold cross validation method is used and the accuracy is calculated to measure its performance.
- (iv) Use three benchmark datasets in experiments where these dataset obtain from University of California, Irvine (UCI) machine learning repository which are the cancer dataset, diabetes dataset and flower dataset.
- (v) In order to measure the performance of the proposed method, it will be compared with several works in the fuzzy modeling.

1.6 Significance of the Study

Fuzzy modeling can be viewed as a grey-box modeling because it allows the modeler to extract and interpret the knowledge that is contained in the data and also to imbue it with a prior knowledge (Babuska and Verbruggen, 1996; Reyes and Sipper, 2002). It is difficult to apply the fuzzy system on complex problems due to the requirement of the system. This is because the representation of the solution becomes more complex and difficult to understand by the human knowledge. Because of that, this study applies learning and tuning capabilities of GA, and decomposes method that is inspired by the CooCEA. With the learning and tuning capabilities of GA, the process of altering and adjusting the fuzzy model can be performed automatically. Meanwhile, the CooCEA is able to decompose the component in fuzzy model into sub-components thus can reduce the complexity of the representation of the solution. Therefore, the significance of this study is to create a method that automate the fuzzy modeling where the generation process of the fuzzy model can be performed automatically, and produce a fuzzy model that took into account the accuracy and interpretability of the model. As a consequence, it can help and facilitate computer scientists to produce computer expert systems such as the application to detect the breast cancer in patients.

1.7 Structure of the Thesis

This thesis is organized into six chapters. General content descriptions of subsequent chapters in this thesis are given as follows:

- (i) Chapter 1 describes the background of the study, challenges in the fuzzy modeling, statement of the problem, objectives, significance and scope of the study.

- (ii) Chapter 2 reviews the domain of this study which includes the review of the fuzzy system, the fuzzy modeling, approaches of fuzzy modeling and the advance methods in the fuzzy modeling.
- (iii) Chapter 3 begins with the review of the research activity. Following that is the discussion of the proposed method and the review of the benchmark datasets involved. Besides that, the experimental environment is also discussed.
- (iv) Chapter 4 describes the steps involved in the proposed method. This includes the representation of the cooperative chromosome, fitness evaluation and the reproduction process.
- (v) Chapter 5 discusses the experimental result, discussion and analysis of the proposed method. First and foremost, the results of the experiments are presented. Then it is followed by the discussion section which elaborates the contributions of this study and finally the analysis of the proposed method.
- (vi) Chapter 6 concludes the study and presents the contributions. The future works of the study are also discussed.

REFERENCES

- Abonyi, J., Roubos, J. A. and Szeifert, F. (2003). Data-Driven Generation of Compact, Accurate, and Linguistically Sound Fuzzy Classifiers Based on a Decision-Tree Initialization. *International Journal of Approximate Reasoning*. 32(1), 1-21.
- Akay, M. F. (2009). Support Vector Machines Combined with Feature Selection for Breast Cancer Diagnosis. *Expert Systems with Applications*. 36(2), 3240-3247.
- Alcala-Fdez, J. Alcala, R., Gacto, M., J. and Herrera, F. (2009). Learning the Membership Function Contexts for Mining Fuzzy Association Rules by Using Genetic Algorithms. *Fuzzy Sets and Systems*. 160(7), 905-921.
- Alcala-Fdez, J., Herrera, F., Marquez, F. and Peregrin, A. (2007). Increasing Fuzzy Rules Cooperation Based on Evolutionary Adaptive Inference Systems. *International Journal of Intelligent Systems*. 22(9), 1035-1064.
- Alcala, R., Alcala-Fdez, R., Herrera, F. and Otero, J. (2007). Genetic Learning of Accurate and Compact Fuzzy Rule Based Systems Based on the 2-Tuples Linguistic Representation. *International Journal of Approximate Reasoning*. 44(1), 45-64.
- Alba, E. and Luque, G. (2007). Designing a Parallel GA for Large Instances of the Workforce Planning Problem. *Proceedings of the Seventh International Conference on Intelligent Systems Design and Applications*. 22-24 October. Washington, USA, 823-830.
- Amelia, L., Wahab, D. A. and Hassan, A. (2009). Modeling of Palm Oil Production Using Fuzzy Expert System. *Expert Systems with Applications*. 36(5), 8735-8749.

- Ang, K. K. and Quek, C. (2005). RSPOP: Rough Set-Based Pseudo Outer-Product Fuzzy Rule Identification Algorithm. *Neural Computation*. 17(1), 205-243.
- Asmuni, H. (2008). *Fuzzy Methodologies for Automated University Timetabling Solution Construction and Evaluation*. Ph.D Thesis. University of Nottingham, UK.
- Axelrod, R. (2006), *The Evolution of Cooperation* (Revised ed.). New York, USA: Basic Books.
- Babuska, R. and H. B. Verbruggen (1996). An Overview of Fuzzy Modeling for Control. *Control Engineering Practice*. 4(11), 1593-1606.
- Basu, M. (2007). Dynamic Economic Emission Dispatch Using Evolutionary Programming and Fuzzy Satisfying Method. *International Journal of Emerging Electric Power Systems*. 8(4), doi: 10.2202/1553-779X.1146
- Berlanga, F. J., Rivera, A. J., del Jesus, M. J. and Herrera, F. (2010). GP-COACH: Genetic Programming-Based Learning of Compact and Accurate Fuzzy Rule-Based Classification Systems for High-Dimensional Problems. *Information Sciences*. 180(8), 1183-1200.
- Berry, H. and Temam, O. (2007). Modeling Self-Developing Biological Neural Networks. *Neurocomputing*. 70(16-18), 2723-2734.
- Bevilacqua, V., Grasso, E., Mastronardi, G. and Riccardi, L. (2006). A Soft Computing Approach to the Intelligent Control. *Proceedings of the IEEE International Conference on Industrial Informatics*. 16-18 August. Singapore, 1312-1317.
- Bosl, W. J. (2007). System Biology by the Rules: Hybrid Intelligent Systems for Pathway Modeling and Discovery. *BMC System Biology*. 1(13), doi:10.1186/1752-0509-1-13.
- Casillas, J., Cordon, O., del Jesus, M. J., and Herrera, F. (2005). Genetic Tuning of Fuzzy Rule Deep Structures Preserving Interpretability for Linguistic Modeling. *IEEE Transactions on Fuzzy System*. 13(1), 13-29.
- Cay, T. and Iscan, F. (2010). Application of Fuzzy Logic in Land Consolidation Activities. *FIG Congress: Facing Challenges - Building the Capacity*. 11-16 April. Sydney, Australia, 1-18.
- Celikyilmaz, A. and Turksen, I. B. (2007). Evolutionary Fuzzy System Models with Improved Fuzzy Functions and its Application to Industrial Process.

- Proceedings of the IEEE International Conference on Systems, Man and Cybernetics*. 7-10 October. Montreal, Canada, 541-546.
- Chan, K. Y., Kwong, C. K. and Fogarty, T. C. (2010). Modeling Manufacturing Processes Using a Genetic Programming-Based Fuzzy Regression with Detection of Outliers. *Information Sciences*. 180(4), 506-518.
- Chang, P. C. and Liu, C. H. (2008). A TSK Type Fuzzy Rule Based System for Stock Price Prediction. *Expert Systems with Applications*. 43(1), 135-144.
- Chen, B. S., Feng, S. C., and Wang, K. C. (2000). Traffic Modeling, Prediction, and Congestion Control for High-Speed Networks: A Fuzzy AR Approach. *IEEE Transactions on Fuzzy Systems*. 8(5), 491-508.
- Chen, Y., Yang, B., Abraham, A. and Peng, L. (2007). Automatic Design of Hierarchical Takagi-Sugeno Type Fuzzy Systems Using Evolutionary Algorithms. *IEEE Transactions on Fuzzy Systems*. 15(3), 385-397.
- Chien, B. C., Lin, J. Y. and Hong, T. P. (2002). Learning Discriminant Functions with Fuzzy Attributes for Classification Using Genetic Programming. *Expert Systems with Applications*. 23(1), 31-37.
- Chowdhury, N.A., Khatun, M. and Hashem, M.M.A. (2007). On Integrating Fuzzy Knowledge Using a Novel Evolutionary Algorithm. *Proceedings of the 10th International Conference on Computer and Information Technology*. 27-29 December. Dhaka, Bangladesh, 1-6.
- Cordon, O., Gomide, F., Herrera, F., Hoffmann, F. and Magdalena, L. (2004). Ten Years of Genetic Fuzzy Systems: Current Framework and New Trends. *Fuzzy Sets and Systems*. 141(1), 5-31.
- Cordon, O., Herrera, F., Hoffmann, F. and Magdalena, L. (2001). *Genetic Fuzzy Systems: Evolutionary Tuning and Learning of Fuzzy Knowledge Bases*. Singapore: World Scientific.
- Cornelis, C., Jensen, R., Hurtado, G. and Slezak, D. (2010). Attribute Selection with Fuzzy Decision Reducts. *Information Sciences*. 180(2), 209-224.
- Crockett, K., Bandar, Z., Mclean, D. and O'Shea, J. (2006). On Constructing a Fuzzy Inference Framework Using Crisp Decision Trees. *Fuzzy Sets and Systems*. 157(21), 2809-2832.
- Darwin, C. (2007). *On the Origin of Species: By Means of Natural Selection Or the Preservation of Favored Races in the Struggle for Life*. (reprint). New York, USA: Cosimo, Inc.

- Darwin, C. (2007). *Fertilisation of Orchids*. (reprint). New York, USA: Cosimo, Inc.
- del Jesus, M. J., Gonzalez, P., Herrera, F., Mesonero, M. (2007). Evolutionary Fuzzy Rule Induction Process for Subgroup Discovery: A Case Study in Marketing. *IEEE Trans Fuzzy System* 15(4), 578-592.
- D'Ambrosio, D., Spataro, W. and Iovine, G. (2006). Parallel Genetic Algorithms for Optimising Cellular Automata models of Natural Complex Phenomena: An Application to Debris Flows. *Computers & Geosciences* 32(7), 861-875
- Deng, X. and Wang, X. (2009). Incremental Learning of Dynamic Fuzzy Neural Networks for Accurate System Modeling. *Fuzzy Sets and Systems*. 160(7), 972-987.
- Dimitriou, L., Tsekeris, T. and Stathopoulos, A. (2008). Adaptive Hybrid Fuzzy Rule-Based System Approach for Modeling and Predicting Urban Traffic Flow. *Transportation Research Part C*. 16(5), 554-573.
- Efe, M. O. and Kaynak, O. (2000). On Stabilization of Gradient-Based Training Strategies for Computationally Intelligent Systems. *IEEE-Transactions on Fuzzy Systems*. 8(5), 564-575.
- Efendigil, T., Onut, S. and Kahraman, C. (2009). A Decision Support System for Demand Forecasting with Artificial Neural Networks and Neuro-Fuzzy Models: A Comparative Analysis. *Expert Systems with Applications*. 36(3), 6697-6707.
- El-Midany, T. T., El-Baz, M. A. and Abd-Elwahed, M. S. (2010). A Proposed Framework for Control Chart Pattern Recognition in Multivariate Process Using Artificial Neural Networks. *Expert Systems with Applications*. 37(2), 1035-1042.
- Espinosa, J. and Vandewalle, J. (2000). Constructing Fuzzy Models with Linguistic Integrity from Numerical Data-AFRELI Algorithm. *IEEE Transactions on Fuzzy Systems*. 8(5), 591-600.
- Evsukoff, A. G., Galichet, S., de Lima, B. S. L. P. and Ebecken, N. F. F. (2009) Design of Interpretable Fuzzy Rule-Based Classifiers Using Spectral Analysis with Structure and Parameters Optimization. *Fuzzy Sets and Systems*. 160(7), 857-881.
- Fernandez, A., del. Jesus, M. J., and Herrera, F. (2009). Hierarchical Fuzzy Rule Based Classification Systems with Genetic Rule Selection for Imbalanced Data-Sets. *International Journal of Approximate Reasoning*. 50(3), 561-577

- Fogel, L. J. (1962). Autonomous Automata. *Industrial Research*. 4(2), 14-19.
- Gabryel, M. and Rutkowski, L. (2006). Evolutionary Learning of Mamdani-Type Neuro-Fuzzy Systems. *Proceedings of the International Conference on Artificial Intelligence and Soft Computing*. 25-29 June. Zakopane, Poland, 354-359.
- Gadaras, I. and Mikhailov, L. (2009). An Interpretable Fuzzy Rule-Based Classification Methodology for Medical Diagnosis. *Artificial Intelligence in Medicine*. 47(1), 25-41.
- Ganoulis, J. (2007). *Fuzzy Modelling for Uncertainty Propagation and Risk Quantification in Environmental Water Systems*. In Skanata, D. and Byrd, D. M. (Ed.) *Computational Models of Risks to Infrastructure*. (pp. 260-272). Amsterdam, Netherlands: IOS Press.
- Ghazavi, S. N. and Liao, T. W. (2008). Medical Data Mining by Fuzzy Modeling with Selected Features. *Artificial Intelligence in Medicine*. 43(3), 195-206.
- Gurel, T., Raedta, L. D. and Rottera, S. (2007). Ranking Neurons for Mining Structure-Activity Relations in Biological Neural Networks: NeuronRank. *Neurocomputing*. 70(10-12), 1897-1901.
- Gurel, T., Rotter, S. and Egerty U. (2009). Functional Identification of Biological Neural Networks using Reservoir Adaptation for Point Processes. *Journal of Computational Neuroscience*. doi: 10.1007/s10827-009-0176-0.
- Hamam, A. and Georganas, N. D. (2008). Comparison of Mamdani and Sugeno Fuzzy Inference Systems for Evaluating the Quality of Experience of Haptic-Audio-Visual Applications. *Proceedings of the IEEE International Workshop on Haptic Audio visual Environments and Games*. 18-19 October. Ottawa, Canada, 87-92.
- Herrera, F. (2008). Genetic Fuzzy Systems: Taxonomy, Current Research Trends and Prospects. *Evolutionary Intelligence*. doi: 10.1007/s12065-007-0001-5.
- Holland, J. H. (1962). Outline for a Logical Theory of Adaptive Systems. *Journal of the ACM*. 9 (3), 297-314.
- Homaifar, A., McCormick, E. (1995) Simultaneous Design of Membership Functions and Rule Sets for Fuzzy Controllers using Genetic Algorithms. *IEEE Transactions on Fuzzy Systems*. 3(2), 129-139.

- Hong, T-P., Chen C-H., Lee, Y-C. and Wu, Y-L. (2008). Genetic-Fuzzy Data Mining With Divide-and-Conquer Strategy. *Evolutionary Computation, 2007. CEC 2007*. 2(12), 252-265.
- Hu, Y. C. (2008). Nonadditive Grey Single-Layer Perceptron with Choquet Integral for Pattern Classification Problems Using Genetic Algorithms. *Neurocomputing*. 72 (1-3), 331-340.
- Hwang, G. H., Kim, D. W., Lee, J. H. and An, Y. J. (2008). Design of Fuzzy Power System Stabilizer Using Adaptive Evolutionary Algorithm. *Engineering Applications of Artificial Intelligence*. 21(1), 86-96.
- Hwang, S. F. and He, R. S. (2006). A Hybrid Real-Parameter Genetic Algorithm for Function Optimization. *Advanced Engineering Informatics*. 20(1), 7-21.
- Jang, J. S. R. and Sun, C. T. (1995). Neuro-Fuzzy Modeling and Control. *Proceedings of the IEEE*, 83(3), 378-406.
- Jie, Z. and Hui, J. (2006). Evolutionary Programming Based on Ladder-changed Mutation for Adaptive System Recognition. *Proceedings of the International Conference on Communications, Circuits and Systems Proceedings*. 25-28 June. Guilin, China, 181-184.
- Jin, Y. (2000). Fuzzy Modeling of High-Dimensional Systems: Complexity Reduction and Interpretability Improvement. *IEEE Transactions on Fuzzy Systems*. 8(2), 335-344.
- Kahramanli, H. and Allahverdi, N. (2008). Design of a Hybrid System for the Diabetes and Heart Diseases. *Expert Systems with Applications*. 35(1-2), 82-89.
- Kelesoglu, O. (2007) Fuzzy Multiobjective Optimization of Truss-Structures Using Genetic Algorithm. *Advances in Engineering Software*. 38(10), 717-721.
- Keshwani, D. R., Jones, D. D., Meyer, G. E. and Brand, R. M. (2008). Rule-Based Mamdani-Type Fuzzy Modeling of Skin Permeability. *Applied Soft Computing*. 8(1), 285-294.
- Kim, D., Choi, Y. and Lee, S. (2002). An Accurate COG Defuzzifier Design Using Lamarckian Co-Adaptation of Learning and Evolution. *Fuzzy Sets and System*. 130(2), 207-225.
- Kim, D. W. and Park, G. T. (2005). Using Interval Singleton Type 2 Fuzzy Logic System in Corrupted Time Series Modelling. *Proceedings of the International*

- Conference on Knowledge-Based Intelligent Information and Engineering Systems*. 14-16 September. Melbourne, Australia, 566-572.
- Kim, M. W. and Ryu, J. W. (2005). Optimized Fuzzy Classification Using Genetic Algorithm. *Proceedings of the Second International Conference on Fuzzy Systems and Knowledge Discovery*. 27-29 August. Changsha, China, 392-401.
- Kolman, E. and Margaliot, M. (2009). Extracting Symbolic Knowledge from Recurrent Neural Networks: A Fuzzy Logic Approach. *Fuzzy Sets and Systems*. 160(2), 145-161.
- Kukkurainen, P. and Luukka, P. (2008). Classification Method Using Fuzzy Level Set Subgrouping. *Expert Systems with Applications*. 34(2), 859-865.
- Kordon, A. K. (2010). *Applying Computational Intelligence : How to Create Value*. Heidelberg, Germany: Springer.
- Kothamasu, R. and Huang, S. H. (2007). Adaptive Mamdani Fuzzy Model for Condition-Based Maintenance. *Fuzzy Sets and Systems*. 158(24), 2715-2733.
- Koza, J.R. (1999). *Genetic Programming III; Darwinian Invention and Problem Solving*. San Francisco, USA: Morgan Kaufman.
- Lau H. C. W., Tang C. X. H., Ho G. T. S., and Chan T. M. (2009). A Fuzzy Genetic Algorithm for the Discovery of Process Parameter Settings using Knowledge Representation. *Expert Systems with Applications*. 36(4), 7964-7974.
- Li, M. and Wang, Z. (2009). A Hybrid Coevolutionary Algorithm for Designing Fuzzy Classifiers. *Information Sciences*. 179(12), 1970-1983.
- Li, T. H. S., Guo, N. R. and Cheng, C. P. (2008). Design of a Two-Stage Fuzzy Classification Model. *Expert Systems with Applications*. 35(3), 1482-1495.
- Li, T. H. S., Guo, N. R. and Kuo, C. L. (2005). Design of Adaptive Fuzzy Model for Classification Problem. *Engineering Applications of Artificial Intelligence*. 18(3), 297-306.
- Liu, W., Liang, Z., Huang, T., Chen, Y. and Lian, J. (2008). Process Optimal Control of Sheet Metal Forming Springback Based on Evolutionary Strategy. *Proceedings of the World Congress on Intelligent Control and Automation*. 25-27 June. Chongqing, China, 7940-7945.
- Luukka, P. (2009). Classification Based on Fuzzy Robust PCA Algorithms and Similarity Classifier. *Expert Systems with Applications*. 36(4), 7463-7468.

- Majewski, M. and Zurada, J. M. (2008). Sentence Recognition Using Artificial Neural Networks. *Knowledge-Based Systems*. 21(7), 629-635.
- Mamdani, E. H. and Assilian, S. (1975). An Experiment in Linguistic Synthesis with a Fuzzy Logic Controller. *International Journal of Man-Machine Studies*. 7(1), 1-13.
- Mantas, C. J. and Puche, J. M. (2008). Artificial Neural Networks are Zero-Order TSK Fuzzy Systems. *IEEE Transactions on Fuzzy Systems*. 16(3), 630-643.
- Maeda, Y., Ishita, M. and Li, Q. (2006). Fuzzy Adaptive Search Method for Parallel Genetic Algorithm with Island Combination Process. *International Journal of Approximate Reasoning*. 41(1), 59-73.
- Mao, Y., Tang, W., Lui, Y. and Kocarev, L. (2008). Identification of Biological Neurons Using Adaptive Observers. *Cognitive Processing*. doi: 10.1007/s10339-008-0230-2.
- Marks, R. E. and Schnabl, H. (1999). Genetic Algorithms and Neural Networks: A Comparison Based on the Repeated Prisoners Dilemma. *Advances In Computational Economics*. 11, 197-220.
- Maynard-Smith J. (1982). *Evolution and the Theory of Games*. Cambridge, UK: Univ. Press.
- Mendonca, L. F., Sousa, J. M. C. and Costa, J. M. G. S. (2009). An Architecture for Fault Detection and Isolation Based of Fuzzy Methods. *Expert Systems with Applications*. 36(2), 1092-1104.
- Michalewicz, Z. (1996). *Genetic Algorithms + Data Structures = Evolution Programs* (3rd ed.). Heidelberg, Germany: Springer-Verlag.
- Mikut, R., Jakel, J. and Groll, L. (2005). Interpretability Issues in Data-Based Learning of Fuzzy Systems. *Fuzzy Sets and Systems*. 150(2), 179-197.
- Mohebbi, M., Barouei, J., Akbarzadeh, T. M. R., Rowhanimanesh, A. R., Habibi-Najafi, M. B. and Yavarmanesh, M. (2008). Modeling and Optimization of Viscosity in Enzyme-Modified Cheese by Fuzzy Logic and Genetic Algorithm. *Computers and Electronics in Agriculture*. 62(2), 260-265.
- Nauck, D. and Kruse, R. (1997). A Neuro-Fuzzy Method to Learn Fuzzy Classification Rules from Data. *Fuzzy Sets and Systems*. 89(3), 277-288.
- Negnevitsky, M. (2002). *Artificial Intelligence: A guide to Intelligent System* (2nd ed.). Harlow, UK: Addison Wesley.

- Potter, M. A. and De Jong, K. A. (2000). Cooperative Coevolution: An Architecture for Evolving Coadapted Subcomponents. *Evolutionary Computation*. 8(1), 1-29.
- Prasanna, T. S. and Somasundaram, P. (2008). Fuzzy Mutated Evolutionary Programming Based Algorithm for Combined Economic and Emission Dispatch. *Proceedings of the 2008 IEEE Region 10 Conference TENCON*. 19-21 November. Hyderabad, India, 1-5.
- Pruyt, E., W. Thissen, and Meijer, I. (2008). Dealing with Uncertainties? Combining System Dynamics with Multiple Criteria Decision Analysis or with Exploratory Modelling. *Proceedings of the International Conference on Infrastructure Systems*. 10-12 November. Rotterdam, Netherlands, 1-6.
- Pulkkinen, P., Hytonen, J. and Koivisto, H. (2008). Developing a Bioaerosol Detector Using Hybrid Genetic Fuzzy Systems. *Engineering Applications of Artificial Intelligence*. 21(8), 1330-1346.
- Ramik, J. (2001). *Soft Computing: Overview and Recent Developments in Fuzzy Optimization*. Ph.D Thesis. University of Ostrava, Czech Republic.
- Reyes, C. A. P. and Sipper, M. (2002). Fuzzy CoCo: A cooperative Coevolutionary Approach to Fuzzy Modeling. *IEEE Transactions on Fuzzy Systems*. 9(2), 727-736.
- Reynolds, R. G. and Zhu, S. (2001). Knowledge-Based Function Optimization Using Fuzzy Cultural Algorithms with Evolutionary Programming. *IEEE Transaction On Systems, Man, And Cybernetics-Part B: Cybernetics*. 31(1), 1-18.
- Riid, A. and Rustern, E. (2003). Gradient Descent Based Optimization of Transparent Mamdani Systems. *Proceedings of the Conference on Artificial Intelligence and Applications*. 8-10 September. Benalmadena, Spain, 545-550.
- Rojas, I., Pomares, H., Ortega, J. and Prieto, A. (2000). Self-Organized Fuzzy System Generation from Training Examples. *IEEE Transactions on Fuzzy Systems*. 8(1), 23-36.
- Sazonov, E. S., Klinkhachorn, P., Gangarao, H. S. and Halabe, U. B. (2002). Fuzzy Logic Expert System for Automated Damage Detection from Changes in Strain Energy Mode Shapes. *Nondestructive Testing and Evaluation*. 18(1), 1-20.

- Schiavo, A. L. and Luciano, A. M. (2001). Powerful and Flexible Fuzzy Algorithm for Nonlinear Dynamic System Identification. *IEEE-Transaction on Fuzzy Systems*. 9(6), 828-835.
- Setiono, R. (2000). Generating Concise and Accurate Classification Rules for Breast Cancer Diagnosis. *Artificial Intelligence in Medicine*. 18(3), 205-219.
- Spears, W. M. and De Jong, K. A. (1990). *Using Neural Networks and Genetic Algorithms as Heuristics for NP-Complete Problems*. MSc Thesis. George Mason University, USA.
- Stavarakoudis, D. G., Theocharis, J. B. and Zalidis, G. C. (2009). *Genetic Fuzzy Rule-Based Classifiers for Land Cover Classification from Multispectral Images*. In Valavanis, K. P. (Ed.) *Applications of Intelligent Control to Engineering Systems*. (pp. 195-221). Netherlands: Springer Netherlands.
- Stephanou, H. E. and Sage, A. P. (1987). Perspectives on Imperfect Information Processing. *IEEE Transactions on Systems, Man, and Cybernetics*. 17(5), 780-798.
- Stylios, C. D., Georgopoulos, V. C., Malandraki, G. A. and Chouliara, S. (2008). Fuzzy Cognitive Map Architectures for Medical Decision Support Systems. *Applied Soft Computing*. 8(3), 1243-1251.
- Tewari, A. and Macdonald, M. U. (2010). Knowledge-Based Parameter Identification of TSK Fuzzy Models. *Applied Soft Computing*. 10(2), 481-489.
- Tsipouras, M. G., Exarchos, T. P. and Fotiadis, D. I. (2008). A Methodology for Automated Fuzzy Model Generation. *Fuzzy Sets and Systems*. 159(23), 3201-3220.
- Upegui, A., Thoma, Y., Sanchez, E., Perez-Urbe, A., Moreno, J. M., Madrenas, J. and Sassatelli, G. (2008). The PERPLEXUS Bio-Inspired Hardware Platform: A flexible and Modular Approach. *International Journal of Knowledge-Based and Intelligent Engineering Systems*. 3 (12). 201-212.
- Vilaplana, M., J., Feliu-Batlle, J. and Lopez-Coronado, J. (2007). A Modular Neural Network Architecture for Step-Wise Learning of Grasping Tasks. *Neural Networks*. 20(5), 631-645.
- Wang, L. X. (1997). *A Course in Fuzzy Systems and Control*, Englewood Cliffs. New Jersey, USA: Prentice-Hall.

- Wang, M. H., Tseng, Y. F., Chen, H. C. and Chao, K. H. (2008). A Novel Clustering Algorithm Based on the Extension Theory and Genetic Algorithm. *Expert Systems with Applications*. 36(4), 8269-8276.
- Wang, R. and Zhang, Z. (2007). Energy Coding in Biological Neural Networks. *Cognitive Neurodynamics*. 1(3), 203-212.
- Wang, Y. F., Wang, D. H. and Chai, T. Y. (2009). Modeling and Control Compensation of Nonlinear Friction Using Adaptive Fuzzy Systems. *Mechanical Systems and Signal Processing*. 23(8), 2445-2457.
- Xing, L. N., Chen, Y. W. and Yang, K. W. (2009). Multi-Population Interactive Coevolutionary Algorithm for Flexible Job Shop Scheduling Problems. *Computational Optimization and Applications*. doi: 10.1007/s10589-009-9244-7.
- Xing, Z. Y., Zhang, Y., Hou, Y. L. and Jia, L. M. (2007). On Generating Fuzzy Systems Based on Pareto Multi Objective Cooperative Coevolutionary Algorithm. *International Journal of Control, Automation, and Systems*. 5(4), 444-455.
- Yager, R. R. and Filev, D. P. (1994). *Essentials of Fuzzy Modeling and Control*. New York, USA: John Wiley & Sons.
- Yang, Z., Tang, K. and Yao, X. (2008). Large Scale Evolutionary Optimization Using Cooperative Coevolution. *Information Sciences*. 178(15), 2985-2999.
- Yazdani, S., Shoorehdeli, M. A. and Tesnehlal, M. (2008). Identification of Fuzzy Models Using Cartesian Genetic Programming. *Proceedings of the 2008 International Conference on Computational Intelligence and Security*. 13-17 December. Suzhou, China, 76-81.
- Yen, J. (1999). Fuzzy Logic-A Modern Perspective. *IEEE Transactions on Knowledge and Data Engineering*. 11(1), 153-165.
- Zadeh, L. A. (1965). Fuzzy Sets. *Information and Control*. 8(3), 338-353.
- Zadeh, L. A. (1973). Outline of a New Approach to the Analysis of Complex Systems and Decision Processes. *IEEE Transactions on Systems, Man and Cybernetics*. 3(1), 28-44.
- Zadeh, L. A. (1975). The Concept of a Linguistic Variable and its Applications to Approximate Reasoning. *Information Science*. 9(1), 43-80.
- Zong-Yi, X., Yuan-Long, H., Yong, Z., Li-Min, J. and Yuexian, H. (2006). A Multi-Objective Cooperative Coevolutionary Algorithm for Constructing Accurate

and Interpretable Fuzzy systems. *Proceedings of the IEEE International Conference on Fuzzy Systems*. 16-21 July. Vancouver, Canada, 1404-1410.

Zhu, F. and Guan, S. U. (2008). Cooperative Co-Evolution of GA-Based Classifiers Based on Input Decomposition. *Engineering Applications of Artificial Intelligence*. 21(8), 1360-1369.